

# VIRTUAL ANTHROPOLOGY AND THE STUDY OF SKELETAL FORM AND FUNCTION

**RICARDO MIGUEL GODINHO** University of York, Department of Archaeology and Hull York Medical School, ricardomiguelgodinho@gmail.com

**RESUMO** A paleoantropologia estuda frequentemente a relação entre forma e função. Tradicionalmente, esses estudos usam morfometria convencional para medir a forma e simplificações geométricas para analisar a função mecânica. A antropologia virtual reúne um conjunto de avanços tecnológicos e disciplinas para melhorar o conhecimento da morfologia esquelética e da sua função mecânica. A morfometria geométrica é já uma área implementada, e frequentemente utilizada na antropologia virtual, que apresenta múltiplas vantagens relativamente à morfometria convencional. A análise de elementos finitos não é normalmente integrada na antropologia virtual mas é crescentemente utilizada em paleoantropologia. Permite simulações mecânicas complexas em esqueletos cujos resultados são decisivos na compreensão de como o esqueleto responde a cargas mecânicas. Este manuscrito apresenta uma revisão geral das técnicas tradicionalmente utilizadas em estudos paleoantropológicos de forma-função e como a antropologia virtual pode melhorar o conhecimento nesta área.

**PALAVRAS CHAVE** Antropologia virtual, morfometria geométrica, análise de elementos finitos, forma-função, paleoantropologia

**ABSTRACT** Many paleoanthropology studies examine skeletal form and function. Those studies have traditionally used conventional morphometrics to measure form and geometrical simplifications to assess mechanical function. Virtual anthropology (VA) gathers a set of technological advances and disciplines to augment understanding of skeletal morphology and mechanical function. Geometric Morphometrics is now a well-established morphometric approach, and commonly used in VA, that offers clear advantages over traditional morphometrics. Finite Element Analysis is not integrated in VA, but has recently started being used in paleoanthropology. It allows complex simulations of mechanical loading, thus providing important insights about how skeletal elements respond to loading. This paper provides a general overview of traditional approaches in paleoanthropology to studies of skeletal form and function and how VA is able improve such approaches.

**KEYWORDS** Virtual anthropology, geometric morphometrics, finite element analysis, form-function, paleoanthropology

## INTRODUCTION

Paleoanthropology has compared cranial form between populations (Coon, 1962; Howels, 1973; Lahr, 1996). When morphological dissimilarities are identified they are often associated with mechanical loading, which has been shown to impact skeletal form (Currey, 2006). Thus, paleoanthropology often focuses mechanical function (Rak, 1983; Russell, 1985; Rak, 1986; Demes, 1987; Trinkaus, 1987; Demes and Creel, 1988; Ruff, 2007). Traditionally, such studies used conventional morphometrics to measure form and geometrical simplifications to measure mechanical function. Virtual anthropology (VA) uses a set of computer based approaches to augment assessment of skeletal form. Instead of examining physical bones, VA uses three dimensional surfaces or volumes to perform analyses that allow comprehensive morphological studies and visualization of internal structures that are physically inac-

cessible without sectioning bone/teeth (Weber, 2015). Morphological analysis in VA typically uses Geometric Morphometrics (GM) to allow a better understanding of morphological variance (Weber, 2015). Moreover, by integrating other techniques currently used in virtual functional morphology, such as Finite Element Analysis (O'Higgins *et al.*, 2011), VA may also enhance the study of human skeletal mechanical function.

Thus, this paper presents an overview of how paleoanthropology typically measured form-function and how VA may improve studies of skeletal form and function.

## MEASURING FORM

Measurement of human form has typically relied on linear measurements, which are basically measures of size. Even though size and shape are intimately linked in biological processes, theory of shape states that form integrates size *and* shape (Zelditch *et al.*, 2004). This

partitioning is relevant when considering the impact of size on shape. The former is a scalar and can be measured in multiple ways. Shape is defined as the geometrical information that is invariant to location, orientation and scale (Zelditch *et al.*, 2004). Thus, in order to examine shape, researchers started using ratios and angles in addition to lengths (Slice, 2005) and traditional morphometrics combined those measurements with multivariate statistics to analyze morphology. However traditional multivariate morphometrics has statistical limitations, does not allow complete encoding of geometry and does not allow visualization of morphology (Adams *et al.*, 2004). To overcome those limitations, morphometrics underwent a revolution in the 1980s and several new techniques were created, of which GM became the most popular (Adams *et al.*, 2004; Slice, 2005).

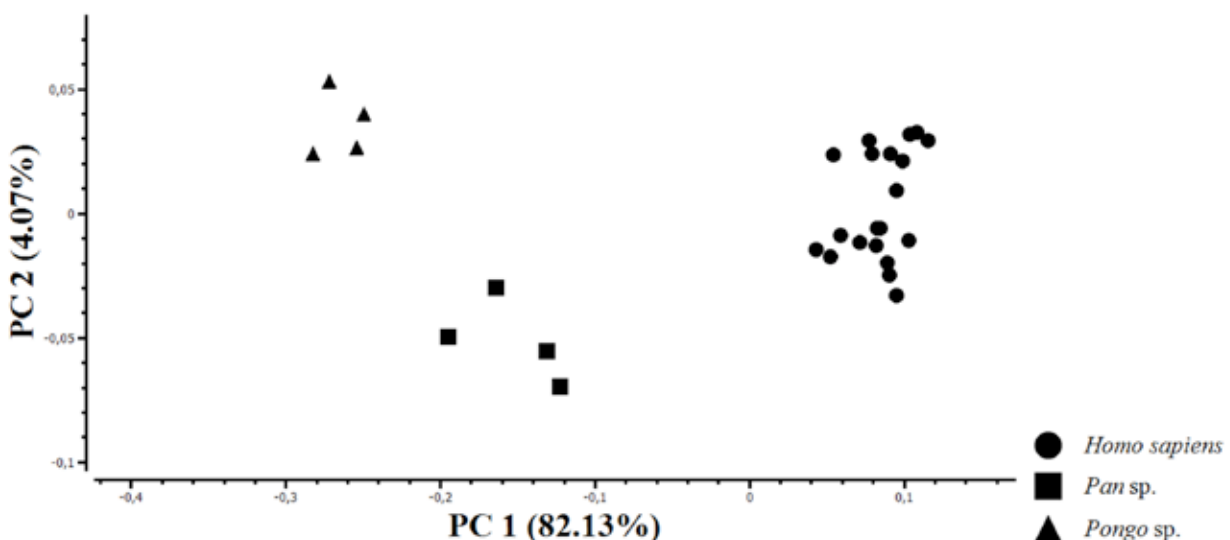
GM has been defined as the statistical analysis of covariation between shape and other causal variables (Bookstein, 1997). To capture form GM relies on landmarks, which are homologous points between specimens assumed to have biological equivalence and relevance (O’Higgins, 2000). However there are not many classical landmarks that can be used to map morphology. Hence, researchers developed sliding semi-landmarks (Gunz and Mitteroecker, 2013), which are geometrically homologous points that allow dense coverage of regions that lack classical landmarks, such as curves and surfaces (figure 1).

The first step in GM is, thus, acquisition of geometry through landmarking, which is commonly done virtually using 3D surfaces. Once landmarking is complete landmark coordinates are submitted to Generalized Procrustes Analysis, which removes the effects of location, scale and orientation (Zelditch *et al.*, 2004). Scaling removes size information and leads to analysis of shape, but size and shape are intimately linked in biological processes. Thus, several approaches have been used to account for size *and* shape (Mitteroecker *et al.*, 2004;



1. Example of reconstructed fossil hominin (Kabwe 1) with 71 classical landmarks (dark grey) and 350 sliding semi-landmarks (light grey).

O’Higgins and Milne, 2013). After registration, analysis is based on multivariate statistics of the shape variables. A standard practice is to perform a principal component analysis, investigate morphological variance (figure 2) and visualize morphological differences using the Thin Plate Spline (TPS) function to warp reference specimens along principal components. This approach has been used to investigate intra and inter-specific morphological differences (Delson *et al.*, 2001; Bastir *et al.*, 2007; Harvati *et al.*, 2010; Baab *et al.*, 2013) and ontogenetic patterns (Collard and O’Higgins, 2001; Cobb and O’Higgins, 2004, 2007; Bastir *et al.*, 2008; Freidline *et al.*, 2012). Multivariate regression has been used to



2. Example of PCA examining morphological variance in *Homo sapiens*, *Pan sp.* and *Pongo sp.*

examine the impact of size on shape (Mitteroecker *et al.*, 2004; Franklin *et al.*, 2007) and of age on mandibular shape (Franklin *et al.*, 2007). Partial least squares has been used in integration and modularity studies (Bastir and Rosas, 2005; Mitteroecker and Bookstein, 2008; Neaux *et al.*, 2015), and to determine the relevance of biomechanical (Noback and Harvati, 2015b; Noback and Harvati, 2015a) and ecological (Monteiro *et al.*, 2003; Noback *et al.*, 2011) factors on form.

### RECONSTRUCTING INCOMPLETE FORMS

Paleoanthropology frequently deals with skeletal elements that are distorted and fragmented. This severely constrains morphology studies, thus researchers have reconstructed incomplete specimens to enable further research. However, physical reconstruction has proved itself detrimental for preservation of fossils (e.g. the Le Moustier Neanderthal cranium). Furthermore, it is a subjective process that involves assumptions and relies on anatomical expertise (Tattersall and Sawyer, 1996; Gunz *et al.*, 2009). This impacts on later research because studies often use casts of those reconstructions (Gunz *et al.*, 2009). VA allows more objective approaches to reconstruction of incomplete specimens and the advantage of being performed virtually, thus not requiring any handling of specimens (Weber, 2015). Virtual reconstruction approaches depend on the aim of subsequent research. When research only requires estimation of missing landmarks this can be done using statistical or geometric based reconstruction. The former uses multivariate regression, which is based on existing landmarks to estimate missing points. Geometric based landmark reconstruction uses the TPS function to estimate missing landmarks (Gunz *et al.*, 2009). However, FEA studies simulating function require complete specimens (see below). In such cases it is necessary to fully reconstruct the missing elements. Symmetry may be used and existing contralateral elements reflected to replace missing structures. Furthermore, because no skeletal structures are perfectly symmetrical, TPS may be used to warp reflected elements to existing structures, thus accounting, to some extent, for asymmetry. When no contralateral elements are present it is possible to use portions of other specimens and warp them to the morphology of the target specimens (Gunz *et al.*, 2009).

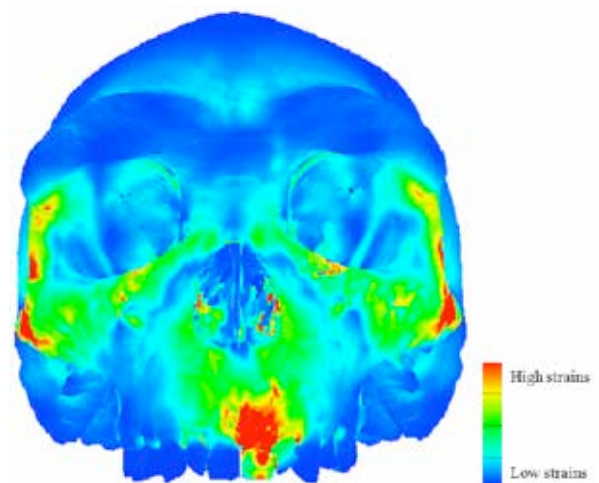
### MEASURING MECHANICAL FUNCTION

Several paleoanthropology studies have focused on assessing how skulls resist biting. Such studies have, until recently, used geometrical simplifications of crania (Rak, 1983; 1986; Demes, 1987; Trinkaus, 1987). Direct strain measurement using strain gauges in other primates (Hylander *et al.*, 1991; Ross and Hylander, 1996; Ravosa *et al.*, 2000a; Ross, 2001) has also been used to infer hominin cranial mechanical function (Ravosa *et al.*, 2000b). Although these approaches are informative and provide insights about how hominin crania resisted biting, they do not allow assessment of

experienced deformations. Thus, with increasing computational power, researchers started using FEA to predict stresses and strains experienced by crania during biting (Strait *et al.*, 2007; Strait *et al.*, 2009; Strait *et al.*, 2010; Wroe *et al.*, 2010; Benazzi *et al.*, 2015; Smith *et al.*, 2015b; Ledogar *et al.*, 2016).

FEA is a numerical tool for solving engineering or mathematical physics problems (Logan, 2007) that has recently been applied to hominin biomechanics to analyze how skeletal elements resist loading (Strait *et al.*, 2007; Strait *et al.*, 2009; Strait *et al.*, 2010; Wroe *et al.*, 2010; Benazzi *et al.*, 2015; Smith *et al.*, 2015b; Ledogar *et al.*, 2016).

FEA requires creation of a model that is divided (discretized) into a set of elements. Models can be based on surface or volume scans and computer-aided design (Richmond *et al.*, 2005), but CT-based models have been recognized as most reliable (Marinescu *et al.*, 2005). Such CT-based models are built through a segmentation process that uses differences in bone density to extract relevant structures from the scanned volume (Weber and Bookstein, 2011). Once the model is created material properties are allocated, forces applied and the model constrained in space. These boundary conditions impact on how the model responds to loading and the strains it experiences. After all boundary conditions are applied the model is solved and resulting displacements calculated. Stresses and strains are commonly used to assess how models respond to loading (figure 3). However, FEA is only useful if results approximate reality, thus a validation phase should also be included when possible (Richmond *et al.*, 2005; Kupczik, 2008). Despite all progress FEA allows in mechanical simulations there is significant debate about what biologically meaningful information may actually be inferred from FEA studies (Weber *et al.*, 2011; Daegling *et al.*, 2013; Strait *et al.*, 2013). Hence, interpretation should be cautious not to assume erroneous conclusions.



3. Example of a solved FE model of a hominin fossil (Kabwe 1) cranium.

## VIRTUAL EXPERIMENTAL MORPHOLOGY

Creation of FE models is an extremely time consuming process. Thus, transforming an existing model into a target form is of significant interest. This can be achieved with good results by densely landmarking an original specimen and warping it into a target that was landmarked similarly (Stayton, 2009; O'Higgins *et al.*, 2011). This approach can also be applied to create models that represent extremes of morphological variance within a taxon. Those models can then be used to simulate mechanical loading and examine how intra-specific morphological variance impacts on mechanical function (Smith *et al.*, 2015a).

Modification of discrete anatomical regions allows creation of experimental specimens that may be of interest (O'Higgins *et al.*, 2011). For example, Strait *et al.* (2007) experimentally thickened the hard palate of a *Macaca fascicularis* and measured resulting strains to infer the relevance of thick palates in Australopithecids. Fitton *et al.* (2009) reconstructed a gracile *Australopithecus* and warped the zygomatic arch to that of a *Paranthropus* while maintaining the remaining anatomy constant. This allowed assessing how changing this region would impact on stresses and strains.

## FINAL REMARKS

With increasing computing power and new technologies VA is able to bring together a set of techniques (e.g. GM and FEA) that augment insights on form and function when compared to traditional paleoanthropology studies. GM allows a deeper understanding of morphology and how it varies intra and inter-specifically. Furthermore, it is also fundamental in the reconstruction of incomplete specimens. FEA allows complex simulations of mechanical function that account for gross morphological complexity, material properties of skeletal structures, force magnitudes and directions of muscles. Thus, by combining these and other computerized techniques VA provides new insights about form-function in paleoanthropology.

## ACKNOWLEDGEMENTS

I am funded by the Portuguese Foundation for Science and Technology (reference SFRH /BD/76375/2011). Prof. Paul O'Higgins for supervising me, all the support and providing me training. Everyone at Centre for Anatomical and Human Sciences (Hull York Medical School, University of York). Gerhard Weber and Fred Bookstein for making available the data used in figure 3 (data from Weber and Bookstein, 2011).

## BIBLIOGRAPHY

- ADAMS, D.; ROHLF, F.; SLICE, D. (2004) – Geometric morphometrics: ten years of progress following the 'revolution'. *Italian Journal of Zoology*, 71: 1, p. 5-16.
- BAAB, K.; MCNULTY, K.; HARVATI, K. (2013) – Homo floresiensis Contextualized: A Geometric Morphometric Comparative Analysis of Fossil and Pathological Human Samples. *Plos One*, 8: 7, p. 69-119.
- BASTIR, M.; ROSAS, A. (2005) – Hierarchical nature of morphological integration and modularity in the human posterior face. *American Journal of Physical Anthropology*, 128: 1, p. 26-34.
- BASTIR, M.; O'HIGGINS, P.; ROSAS, A. (2007) – Facial ontogeny in Neanderthals and modern humans. *Proceedings of the Royal Society B-Biological Sciences*, 274: 1614, p. 1125-1132.
- BASTIR, M.; ROSAS, A.; LIEBERMAN, D.; O'HIGGINS, P. (2008) – Middle cranial fossa anatomy and the origin of modern humans. *Anatomical Record-Advances in Integrative Anatomy and Evolutionary Biology*, 291: 2, p. 130-140.
- BENZAZZI, S.; NGUYEN, H.; KULLMER, O.; HUBLIN, J.-J. (2015) – Exploring the biomechanics of taurodontism. *Journal of Anatomy*, 226: 2, p. 180-188.
- BOOKSTEIN, F. (1997) – *Morphometric Tools for Landmark Data*. Cambridge: Cambridge University Press.
- COBB, S.; O'HIGGINS, P. (2004) – Hominins do not share a common postnatal facial ontogenetic shape trajectory. *Journal of Experimental Zoology Part B-Molecular and Developmental Evolution*, 302B: 3, p. 302-321.
- COBB, S.; O'HIGGINS, P. (2007) – The ontogeny of sexual dimorphism in the facial skeleton of the African apes. *Journal of Human Evolution*, 53: 2, p. 176-190.
- COLLARD, M.; O'HIGGINS, P. (2001) – Ontogeny and homoplasy in the papionin monkey face. *Evolution & Development*, 3: 5, p. 322-331.
- COON, C. (1962) – *The origin of Races*. New York: Knopf.
- CURREY, J. (2006) – *Bones, Structure and Mechanics*. New Jersey: Princeton University Press.
- DAEGLING, D.; JUDEX, S.; OZCIVICI, E.; RAVOSA, M.; TAYLOR, A.; GRINE, F.; TEAFORD, M.; UNGAR, P. (2013) – Viewpoints: Feeding mechanics, diet, and dietary adaptations in early hominins. *American Journal of Physical Anthropology*, 151: 3, p. 356-371.
- DELSON, E.; HARVATI, K.; REDDY, D.; MARCUS, L.; MOWBRAY, K.; SAWYER, G.; JACOB, T.; MARQUEZ, S. (2001) – The Sambungmacan 3 Homo erectus calvaria: A comparative morphometric and morphological analysis. *Anatomical Record*, 262: 4, p. 380-397.
- DEMES, B. (1987) – Another Look at an Old Face – Biomechanics of the Neandertal Facial Skeleton Reconsidered. *Journal of Human Evolution*, 16: 3, p. 297-303.
- DEMES, B.; CREEL, N. (1988) – Bite Force, Diet, and Cranial Morphology of Fossil Hominids. *Journal of Human Evolution*, 17: 7, p. 657-670.
- FITTON, L.; GROENING, F.; COBB, S.; FAGAN, M.; O'HIGGINS, P. (2009) – Biomechanical Significance of Morphological Variation between the Gracile Australopithecus Africanus (Sts5) and Robust Australopithecus Boisei (Oh5). *Journal of Vertebrate Paleontology*, 29, p. 96a-96a.
- FRANKLIN, D.; CARDINI, A.; O'HIGGINS, P.; OXNARD, C.; DADOUR, I. (2007) – Mandibular morphology as an indicator of human subadult age: geometric morphometric approaches.



- Forensic Science, Medicine, and Pathology*, 4: 2, p. 91-99.
- FREIDLINE, S.; GUNZ, P.; HARVATI, K.; HUBLIN, J. (2012) – Middle Pleistocene human facial morphology in an evolutionary and developmental context. *Journal of Human Evolution*, 63: 5, p. 723-740.
- GUNZ, P.; MITTEROECKER, P.; NEUBAUER, S.; WEBER, G.; BOOKSTEIN, F. (2009) – Principles for the virtual reconstruction of hominin crania. *Journal of Human Evolution*, 57: 1, p. 48-62.
- GUNZ, P.; MITTEROECKER, P. (2013) – Semilandmarks: a method for quantifying curves and surfaces. *Hystrix, the Italian Journal of Mammalogy*, 24: 1, p. 103-109.
- HARVATI, K.; HUBLIN, J.; GUNZ, P. (2010) – Evolution of middle-late Pleistocene human cranio-facial form: A 3-D approach. *Journal of Human Evolution*, 59: 5, p. 445-464.
- HOWELS, W. (1973) – *Cranial variation in man: A study by multivariate analysis of patterns of difference among recent human populations*. Cambridge: Peabody Museum of Archaeology and Ethnology, Harvard University (Papers of the Peabody Museum of Archaeology and Ethnology, 67).
- HYLANDER, W.; PICQ, P.; JOHNSON, K. (1991) – Masticatory-Stress Hypotheses and the Supraorbital Region of Primates. *American Journal of Physical Anthropology*, 86: 1, p. 1-36.
- KUPCZIK, K. (2008) – Virtual biomechanics: basic concepts and technical aspects of finite element analysis in vertebrate morphology. *Journal of Anthropological Sciences*, 86, p. 193-198.
- LAHR, M. (1996) – *The evolution of modern human diversity: a study of cranial variation*. Cambridge: Cambridge University Press.
- LEDOGAR, J.; SMITH, A.; BENAZZI, S.; WEBER, G.; SPENCER, M.; CARLSON, K.; MCNULTY, K.; DECHOW, P.; GROSSE, I.; ROSS, C.; RICHMOND, B.; WRIGHT, B.; WANG, Q.; BYRON, C.; CARLSON, K.; DE RUITER, D.; BERGER, L.; TAMVADA, K.; PRYOR, L.; BERTHAUME, M.; STRAIT, D. (2016) – Mechanical evidence that Australopithecus sediba was limited in its ability to eat hard foods. *Nat Commun*, 7, p. 1-9.
- LOGAN, D. (2007) – *A First Course in the Finite Element Method*. Delhi: Thomson.
- MARINESCU, R.; DAEGLING, D.; RAPOFF, A. (2005) – Finite element modeling of the anthropoid mandible: The effects of altered boundary conditions. *Anatomical Record Part a-Discoveries in Molecular Cellular and Evolutionary Biology*, 283A: 2, p. 300-309.
- MITTEROECKER, P.; GUNZ, P.; BERNHARD, M.; SCHAEFER, K.; BOOKSTEIN, F. (2004) – Comparison of cranial ontogenetic trajectories among great apes and humans. *Journal of Human Evolution*, 46: 6, p. 679-697.
- MITTEROECKER, P.; BOOKSTEIN, F. (2008) – The evolutionary role of modularity and integration in the hominoid cranium. *Evolution*, 62: 4, p. 943-958.
- MONTEIRO, L.; DUARTE, L.; DOS REIS, S. (2003) – Environmental correlates of geographical variation in skull and mandible shape of the punare rat *Thrichomys apereoides* (Rodentia: Echimyidae). *Journal of Zoology*, 261, p. 47-57.
- NEAUX, D.; GILISSEN, E.; COUDYZER, W.; GUY, F. (2015) – Integration between the face and the mandible of Pongo and the evolution of the craniofacial morphology of orangutans. *American Journal of Physical Anthropology*, 158: 3, p. 475-486.
- NOBACK, M.; HARVATI, K.; SPOOR, F. (2011) – Climate-related variation of the human nasal cavity. *American Journal of Physical Anthropology*, 145: 4, p. 599-614.
- NOBACK, M.; HARVATI, K. (2015a) – The contribution of subsistence to global human cranial variation. *Journal of Human Evolution*, 80, p. 34-50.
- NOBACK, M.; HARVATI, K. (2015b) – Covariation in the Human Masticatory Apparatus. *The Anatomical Record*, 298: 1, p. 64-84.
- O'HIGGINS, P. (2000) – The study of morphological variation in the hominid fossil record: biology, landmarks and geometry. *Journal of Anatomy*, 197, p. 103-120.
- O'HIGGINS, P.; COBB, S.; FITTON, L.; GRONING, F.; PHILLIPS, R.; LIU, J.; FAGAN, M. (2011) – Combining geometric morphometrics and functional simulation: an emerging toolkit for virtual functional analyses. *Journal of Anatomy*, 218: 1, p. 3-15.
- O'HIGGINS, P.; MILNE, N. (2013) – Applying geometric morphometrics to compare changes in size and shape arising from finite elements analyses. *Hystrix, the Italian Journal of Mammalogy*, 24: 1, p. 126-132.
- RAK, Y. (1983) – The Australopithecine Face. In RAK, Y., ed., *The Australopithecine Face*. New York: Academic Press.
- RAK, Y. (1986) – The Neanderthal – a New Look at an Old Face. *Journal of Human Evolution*, 15: 3, p. 151-164.
- RAVOSA, M.; NOBLE, V.; HYLANDER, W.; JOHNSON, K.; KOWALSKI, E. (2000a) – Masticatory stress, orbital orientation and the evolution of the primate postorbital bar. *Journal of Human Evolution*, 38: 5, p. 667-693.
- RAVOSA, M.; VINYARD, C.; HYLANDER, W. (2000b) – Stressed out: Masticatory forces and primate circumorbital form. *Anatomical Record*, 261: 5, p. 173-175.
- RICHMOND, B.; WRIGHT, B.; GROSSE, L.; DECHOW, P.; ROSS, C.; SPENCER, M.; STRAIT, D. (2005) – Finite element analysis in functional morphology. *Anatomical Record Part a-Discoveries in Molecular Cellular and Evolutionary Biology*, 283A: 2, p. 259-274.
- ROSS, C.; HYLANDER, W. (1996) – In vivo and in vitro bone strain in the owl monkey circumorbital region and the function of the postorbital septum. *American Journal of Physical Anthropology*, 101: 2, p. 183-215.
- ROSS, C. (2001) – In vivo function of the craniofacial haft: The interorbital "pillar". *American Journal of Physical Anthropology*, 116: 2, p. 108-139.
- RUFF, C. (2007) – Biomechanical Analyses of Archaeological Human Skeletons. In KATZENBERG, M.; SAUNDERS, S., eds., *Biological Anthropology of the Human Skeleton*. New York: John Wiley & Sons, Inc., p. 183-206.
- RUSSELL, M. (1985) – The Supraorbital Torus – a Most Remarkable Peculiarity. *Current Anthropology*, 26: 3, p. 337-360.
- SLICE, D. (2005) – Modern morphometrics. In SLICE, D., ed., *Modern morphometrics in physical anthropology*. Berlin: Springer, p. 1-45.
- SMITH, A.; BENAZZI, S.; LEDOGAR, J.; TAMVADA, K.; PRYOR SMITH, L.; WEBER, G.; SPENCER, M.; DECHOW, P.; GROSSE, I.; ROSS, C.; RICHMOND, B.; WRIGHT, B.; WANG, Q.; BYRON, C.; SLICE, D.; STRAIT, D. (2015a) – Biomechanical Implications of Intraspecific Shape Variation in Chimpanzee Crania: Moving Toward an Integration of Geometric Morphometrics and Finite Element Analysis. *The Anatomical Record*, 298: 1, p. 122-144.
- SMITH, A.; BENAZZI, S.; LEDOGAR, J.; TAMVADA, K.; PRYOR SMITH, L.; WEBER, G.; SPENCER, M.; LUCAS, P.; MICHAEL, S.; SHEKEBAN, A.; AL-FADHALAH, K.; ALMUSALAM, A.; DECHOW, P.; GROSSE, I.; ROSS, C.; MADDEN, R.; RICHMOND, B.; WRIGHT, B.; WANG, Q.; BYRON, C.; SLICE, D.; WOOD, S.; DZIALO, C.; BERTHAUME, M.; VAN CASTEREN, A.; STRAIT, D. (2015b) – The Feeding Biomechanics and Dietary Ecology of *Paranthropus boisei*. *The Anatomical Record*, 298: 1, p. 145-167.
- STAYTON, C. (2009) – Application of thin-plate-spline transformations to finite element models, or, how to turn a bog turtle into a spotted turtle to analyze both. *Evolution*, 63: 5, p. 1348-1355.

- STRAIT, D.; RICHMOND, B.; SPENCER, M.; ROSS, C.; DECHOW, P.; WOOD, B. (2007) – Masticatory biomechanics and its relevance to early hominid phylogeny: An examination of palatal thickness using finite-element analysis. *Journal of Human Evolution*, 52: 5, p. 585-599.
- STRAIT, D.; WEBER, G.; NEUBAUER, S.; CHALK, J.; RICHMOND, B.; LUCAS, P.; SPENCER, M.; SCHREIN, C.; DECHOW, P.; ROSS, C.; GROSSE, I.; WRIGHT, B.; CONSTANTINO, P.; WOOD, B.; LAWN, B.; HYLANDER, W.; WANG, Q.; BYRON, C.; SLICE, D.; SMITH, A. (2009) – The feeding biomechanics and dietary ecology of *Australopithecus africanus*. *Proceedings of the National Academy of Sciences of the United States of America*, 106: 7, p. 2124-2129.
- STRAIT, D.; GROSSE, I.; DECHOW, P.; SMITH, A.; WANG, Q.; WEBER, G.; NEUBAUER, S.; SLICE, D.; CHALK, J.; RICHMOND, B.; LUCAS, P.; SPENCER, M.; SCHREIN, C.; WRIGHT, B.; BYFTON, C.; ROSS, C. (2010) – The Structural Rigidity of the Cranium of *Australopithecus africanus*: Implications for Diet, Dietary Adaptations, and the Allometry of Feeding Biomechanics. *Anatomical Record-Advances in Integrative Anatomy and Evolutionary Biology*, 293: 4, p. 583-593.
- STRAIT, D.; CONSTANTINO, P.; LUCAS, P.; RICHMOND, B.; SPENCER, M.; DECHOW, P.; ROSS, C.; GROSSE, I.; WRIGHT, B.; WOOD, B.; WEBER, G.; WANG, Q.; BYRON, C.; SLICE, D.; CHALK, J.; SMITH, A.; SMITH, L.; WOOD, S.; BERTHAUME, M.; BENAZZI, S.; DZIALO, C.; TAMVADA, K.; LEDOGAR, J. (2013) – Viewpoints: Diet and dietary adaptations in early hominins: The hard food perspective. *American Journal of Physical Anthropology*, 151: 3, p. 339-355.
- TATTERSALL, I.; SAWYER, G. (1996) – The skull of “*Sinanthropus*” from Zhoukoudian, China: a new reconstruction. *Journal of Human Evolution*, 31: 4, p. 311-314.
- TRINKAUS, E. (1987) – The Neandertal Face. Evolutionary and Functional Perspectives on a Recent Hominid Face. *Journal of Human Evolution*, 16: 5, p. 429-443.
- WEBER, G.; BOOKSTEIN, F.; STRAIT, D. (2011) – Virtual anthropology meets biomechanics. *Journal of Biomechanics*, 44: 8, p. 1429-1432.
- WEBER, G.; BOOKSTEIN, F. (2011) – *Virtual Anthropology - A Guide for a New Interdisciplinary Field*. Wien: Springer-Verlag.
- WEBER, G. (2015) – Virtual Anthropology. *American Journal of Physical Anthropology*, 156, p. 22-42.
- WROE, S.; FERRARA, T.; MCHENRY, C.; CURNOE, D.; CHAMOLI, U. (2010) – The craniomandibular mechanics of being human. *Proceedings of the Royal Society B-Biological Sciences*, 277: 1700, p. 3579-3586.
- ZELDITCH, M.; SWIDERSKI, D.; SHEETS, H.; FINK, W. (2004) – *Geometric Morphometrics For Biologists: A Primer*. New York: Elsevier.